

A new FEM simulation method of paper materials by using gasket model



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42nd International Iarigai Conference

Helsinki, Finland



List of contents

- ❖ 1. Introduction
- ❖ 2. Materials and methods
- ❖ 3. Results and conclusion
- ❖ 4. Outlook



Introduction ——Research Background



Paper cutting

- Mechanical behaviour of paper
- Through-thickness direction



Paper counting



Book binding



Paper creasing



Paper folding



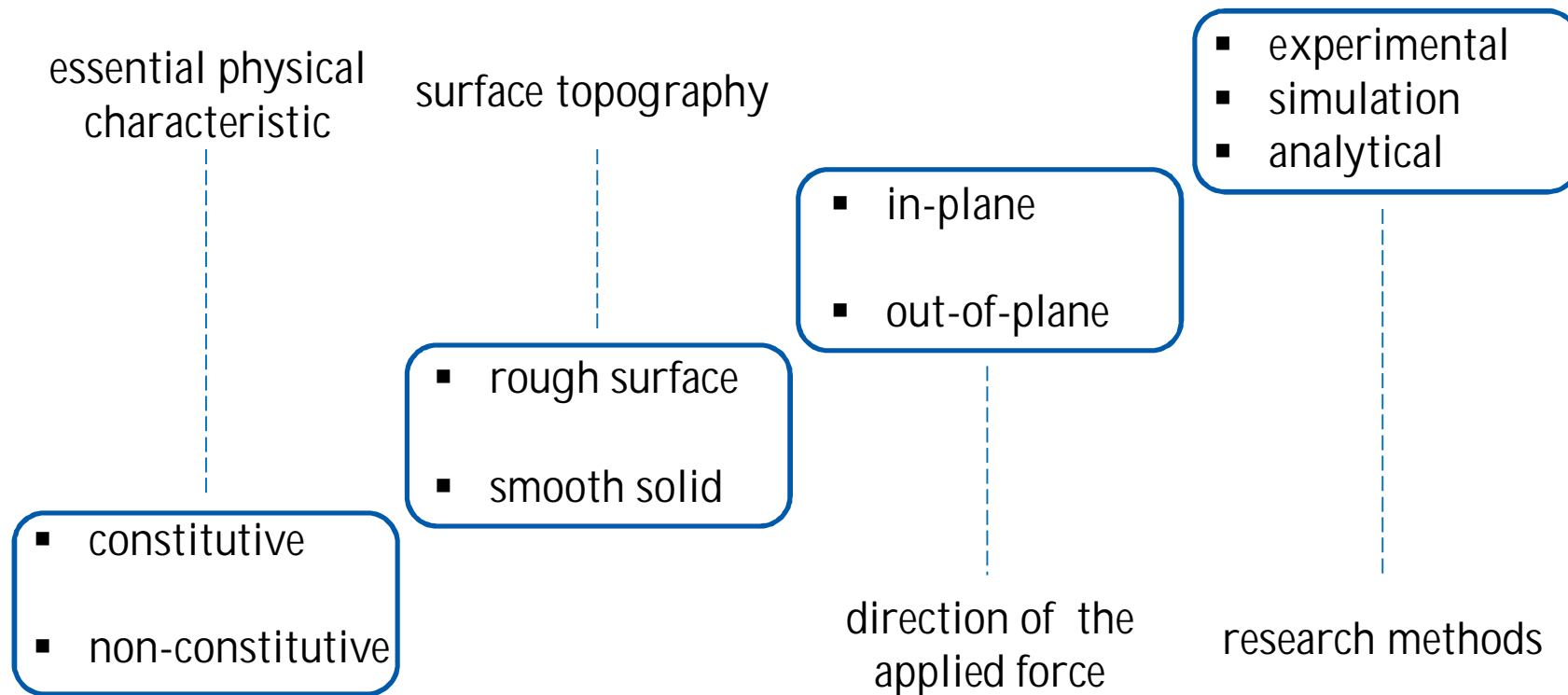
Traditional printing



Paper calendering

Introduction — Paper Models

According to different classification criteria, the paper models can be classified into various groups.



Introduction — Paper Simulation

Research status of paper simulation:

- Still no material model provided which could directly be used for paper simulation.
- Only very few previous works attempt to establish a simulation model.
- Constitutive models require a large number of difficult to measure parameters.
- Extension to multiple sheets is difficult.

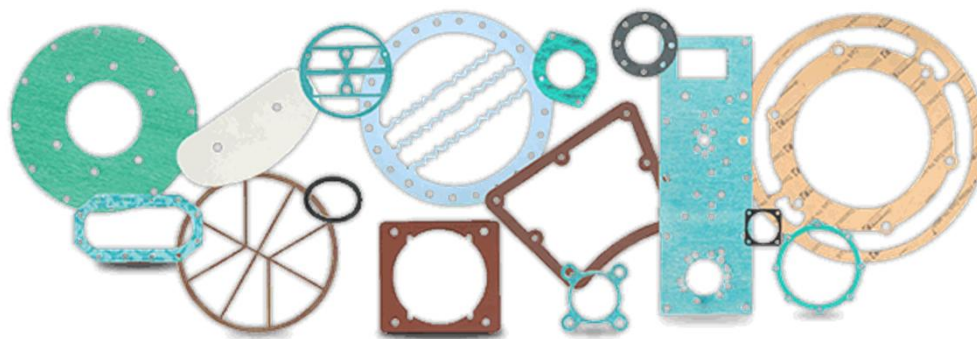


Is it possible to do the simulation of paper materials in a much easier way?

Introduction — Gasket Simulation

Characteristics of gaskets:

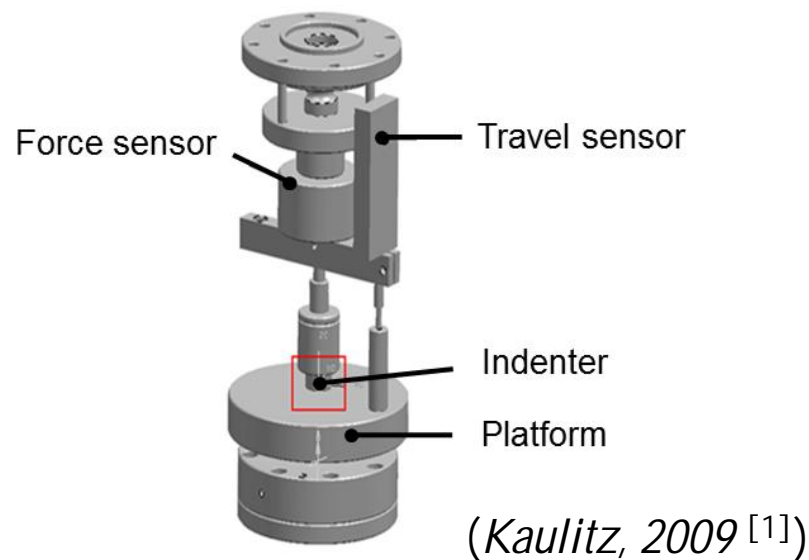
- Thin in one direction, but through-thickness behaviour is most important.
- The mechanical behaviour of gasket in the through-thickness direction is similar to paper materials.
- Gasket elements are offered in FEM software.



How to realize the simulation of paper materials by the gasket model.

Material and Method — Experimental Setup

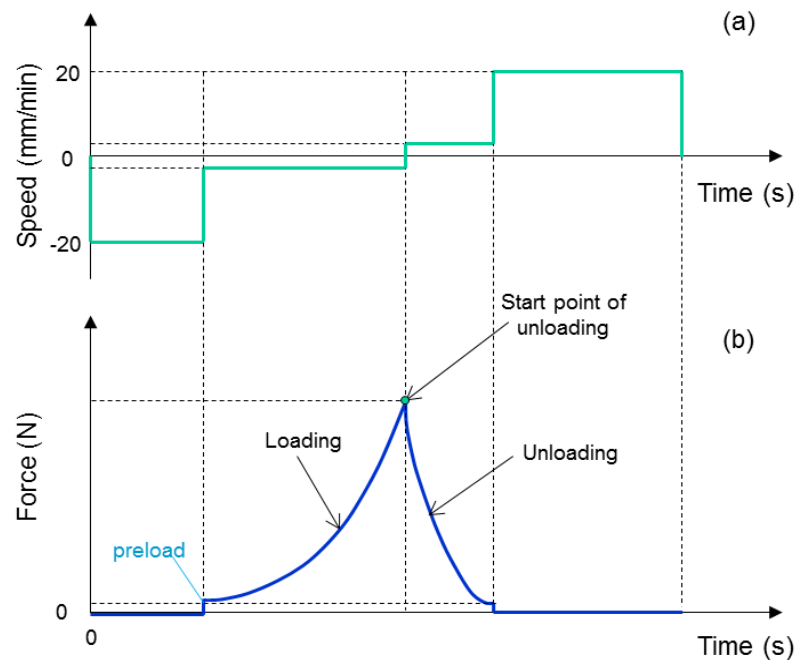
The air-conditioned laboratory of the Institute of Printing Science and Technology (IDD) is equipped with the universal testing machine Zwick Z050.



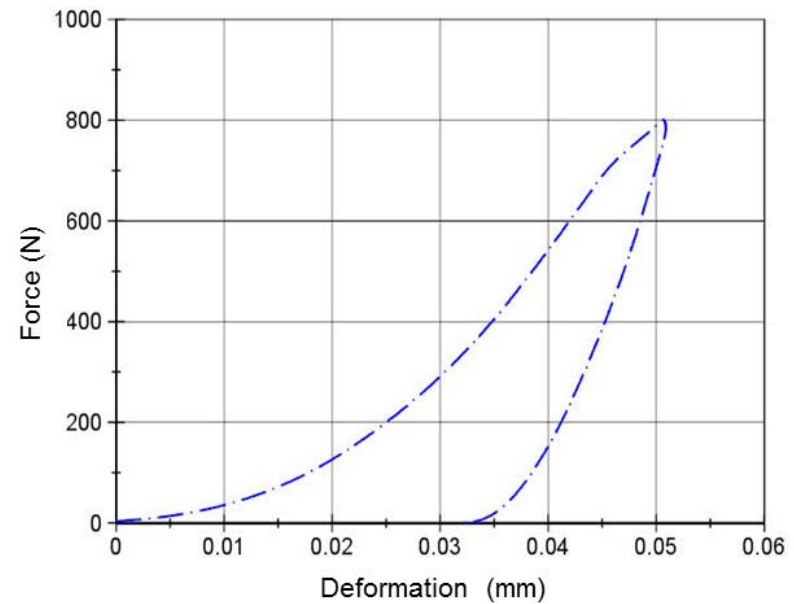
Test equipment for determining force deformation behaviour of paper

- Air-conditioned laboratory of IDD:
 - temperature: $23 \pm 0.5^\circ\text{C}$
 - relative humidity: $50 \pm 1.5\%$
- Parameters of the sample :
 - grammage: 80 g/m^2
 - average thickness: $102 \mu\text{m}$
- Precision accuracy of Zwick machine :
 - cross head speed:
 $0.0005 - 2\,000 \text{ mm/min}$
 - position repetition accuracy:
 $\pm 2 \mu\text{m}$

Experimental Method



Schematic of the applied speed and force in the loading cycle



A typical force-deformation curve of paper

Simulation Process—Fundamental Theory

The definition of the material properties:

- the loading process
- the unloading process

Compressibility model for synthetic gasket material (*Jorwekar, 2006* [2]):

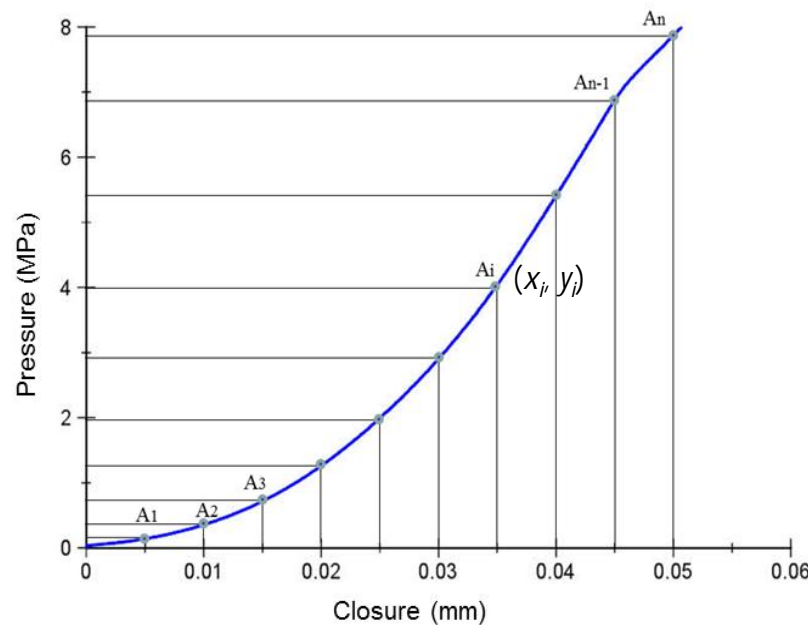
$$y = a \cdot \left(1 - e^{-\left(\frac{x}{b}\right)}\right) + c \cdot \left(1 - e^{-\left(\frac{x}{d}\right)}\right) + u \quad [1]$$

Slope:
$$\frac{dy}{dx} = \left(\frac{a}{b}\right) \cdot e^{-\left(\frac{x}{b}\right)} + \left(\frac{c}{d}\right) \cdot e^{-\left(\frac{x}{d}\right)} \quad [2]$$

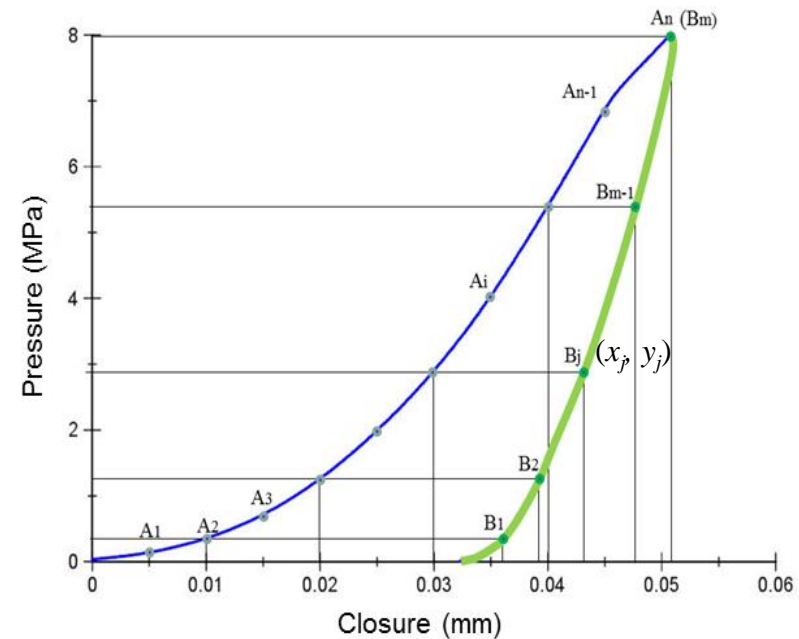
Unloading curve function (due to the unrecoverable strain):

$$u(z) = a \cdot \left(1 - e^{-\left(\frac{z}{b}\right)}\right) + c \cdot \left(1 - e^{-\left(\frac{z}{d}\right)}\right) - \left[a \cdot \left(1 - e^{-\left(\frac{z}{b}\right)}\right) + c \cdot \left(1 - e^{-\left(\frac{z}{d}\right)}\right) \right] \quad [3]$$

Simulation Process — Defining Material Properties

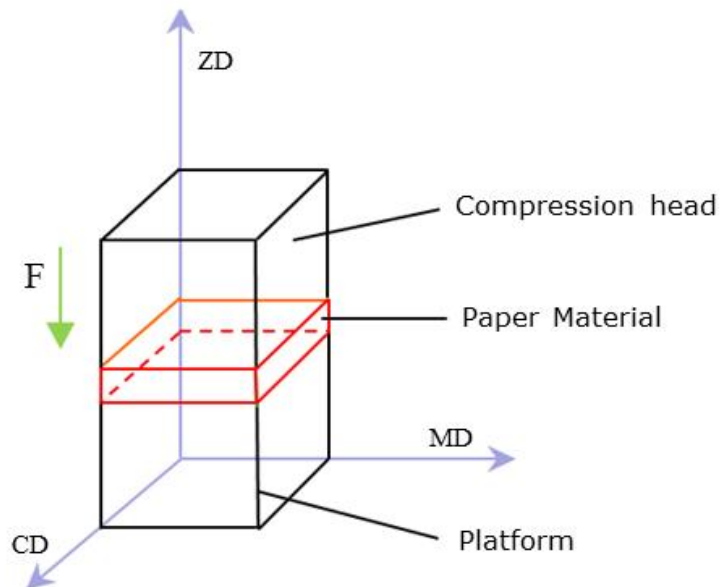


The data selected for defining the loading process



The data selected for defining the unloading process

Simulation Process—Modeling and Simulation



Schematic representation of the simulation model

- i. Defining the material properties
- ii. Building the simulation model
- iii. Meshing the elements
- iv. Defining the constraint conditions
- v. Imposing the force
- vi. Outputting the results

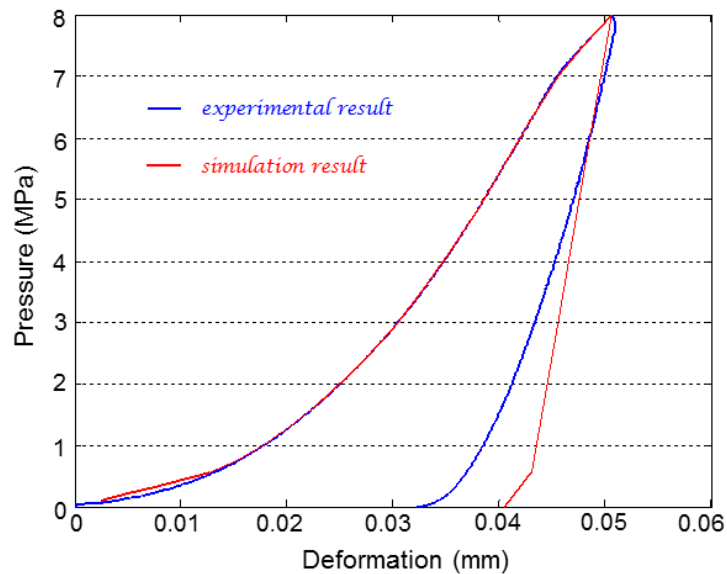


Results and Conclusions

— Paper Simulation under a Defined Force

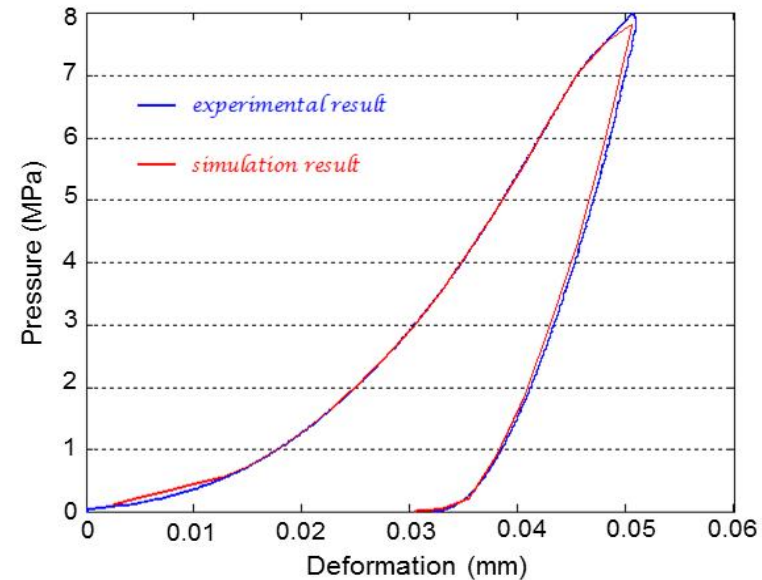
The simulation of paper material finished here:

- the linear unloading simulation
- the non-linear unloading simulation



The linear unloading simulation
result

(A pressure of 8 MPa corresponds to about 800 N)



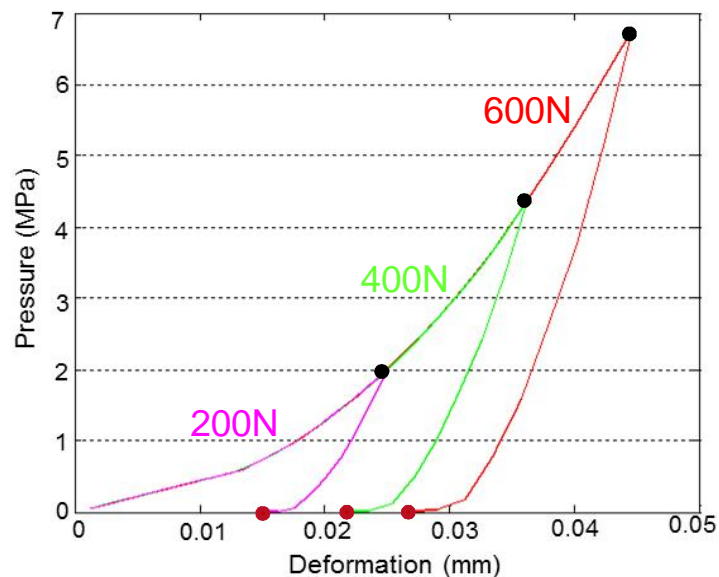
The nonlinear unloading simulation
result

Results and Conclusions

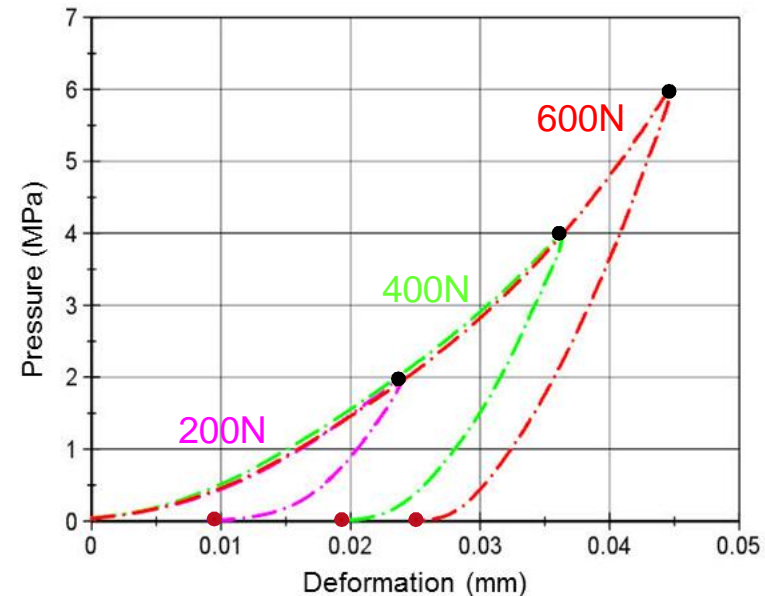
— Simulation under Variable Maximum Forces

Three groups of simulations were implemented:

- the respective maximum forces applied are 200 N, 400 N and 600 N.



The simulation results under different forces



The experimental results under different forces

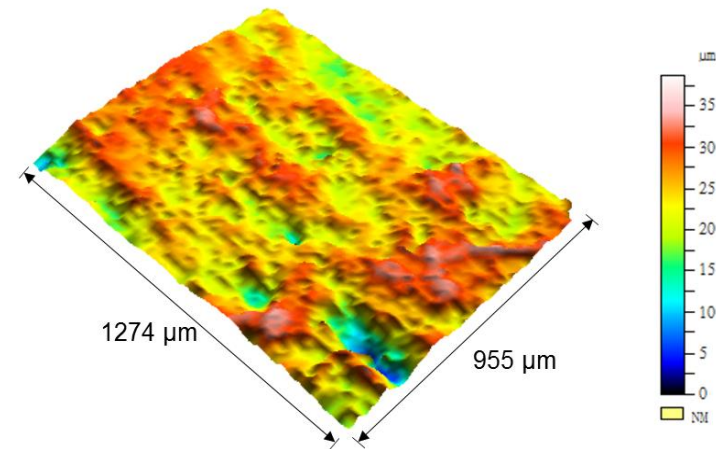
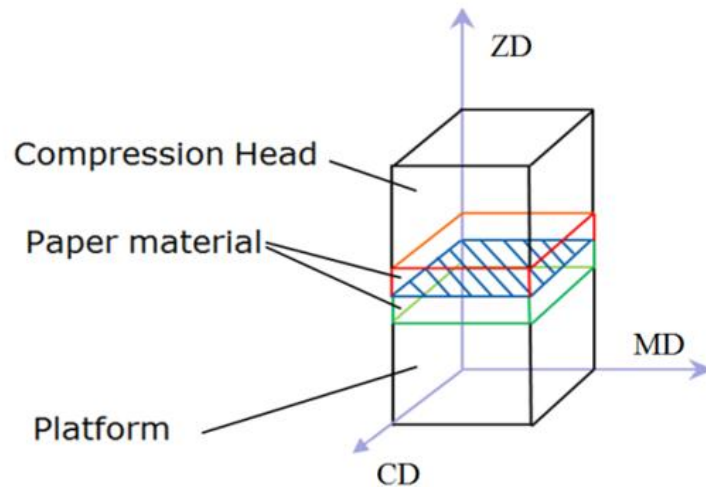
Comparisons between simulations and experiments

Force	200 N	400 N	600 N	800 N
Maximum Pressure (MPa)				
Simulation results	1.82	4.38	6.77	8.00
Experimental results	2.03	4.06	6.09	7.98
Deviation	10.3 %	-7.9%	-11.2%	-0.025%
Residual Strain (-)				
Simulation results	0.14	0.21	0.26	0.30
Experimental results	0.09	0.19	0.24	0.32
Deviation	-64.4 %	-13.5%	-7.7%	6.2%

Conclusions:

- The accuracy of simulation under a specific force is very good.
- The gasket model could be perfectly used for paper simulation.
- To a certain degree, this simulation method could be used for simulations under other forces.

Outlook



One sheet → Two sheets

3D Surface topography of copy paper,
the scan area is 1274 μm × 955 μm.

□ Key problem:

- How to define the contact between paper layers.
- Establishing a model of paper which accounts for the surface topography.

Thanks for your attention!



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- [1] Kaulitz, T., 2009. Bilden von Schneidlagen unter Ausnutzung des Nipinduzierten Effekts für die Druckweiterverarbeitung. (PhD dissertation, Darmstadt University of Technology)*
- [2] Jorwekar, P.P., Birari, Y.V. and Nadgouda, M.M., 2006. Cylinder head gasket contact pressure simulation for a hermetic compressor. International Compressor Engineering Conference at Purdue.*

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